



**University of the Philippines Baguio  
College of Science**

**Department of Mathematics and Computer Science**

# **COURSE SYLLABUS**

**Math 225**

**Number Theory with Applications**



## A. COURSE DETAILS

Course Number:	Math 225										
Course Name:	Number Theory with Applications										
Course Description:	Theory of congruence, Fermat's Theorem, number-theoretic functions, primitive roots and indices, quadratic reciprocity law, perfect numbers, Fermat Conjecture; applications.										
Credit Units:	3 u										
Prerequisite:	COI (Consent of Instructor)										
Requirements:	<table> <tr> <td>Problem Sets, Reporting, Paper, Quizzes,</td> <td></td> </tr> <tr> <td>Class Participation</td> <td>50%</td> </tr> <tr> <td>Midterm Examination</td> <td>25%</td> </tr> <tr> <td>Final Examination</td> <td>25%</td> </tr> <tr> <td><b>Total</b></td> <td><b>100%</b></td> </tr> </table>	Problem Sets, Reporting, Paper, Quizzes,		Class Participation	50%	Midterm Examination	25%	Final Examination	25%	<b>Total</b>	<b>100%</b>
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Class Participation	50%										
Midterm Examination	25%										
Final Examination	25%										
<b>Total</b>	<b>100%</b>										
Passing Grade:	<b>60%</b>										

## B. PROGRAM LEARNING OUTCOMES (PLO)

Upon completion of the MS Mathematics program, the students are able to:

- PLO 1** Discuss advanced concepts from various fields of mathematics including, but not limited to Algebra, Analysis, and Statistics, to exhibit mastery in the different areas of mathematics.
- PLO 2** Provide accurate and rigorous solutions and proofs, both verbal and written, for mathematical problems, to demonstrate deep understanding of the theory and its applications.
- PLO 3** Generate new results to contribute to mathematical knowledge.
- PLO 4** Prepare for doctoral studies, advanced research, and careers in education, industry, and government, towards the students' professional development and personal growth.

## C. COURSE LEARNING OUTCOMES (CLO)

At the end of this course, the students must be able to:

- CLO 1** Discuss and apply advanced concepts and results of Number Theory.
- CLO 2** Effectively communicate ideas on Number Theory in both written and oral forms, including the use of notations and terminology.
- CLO 3** Develop the ability to form conjectures about the integers.
- CLO 4** Demonstrate correct mathematical arguments and proofs, and identify and correct errors in statements.
- CLO 5** Collaborate effectively with a group to address challenging problems in Number Theory.

## D. MAPPING OF CLO with the PLO

	PLO 1	PLO 2	PLO 3	PLO 4
<b>CLO 1</b>	F	F	I	M
<b>CLO 2</b>	F	F	I	M
<b>CLO 3</b>	F	F	M	M
<b>CLO 4</b>	F	F	M	F
<b>CLO 5</b>	F	F	M	F

LEGEND: I-Introduced; M-Moderately achieved; F-Fully achieved



**Introduced [30%, 60%]:** The course has introduced fundamental concepts necessary for the program objectives.  
**Moderately Achieved [60%; 85%]:** The course has developed partial knowledge, somehow prerequisite, for the program objectives.

**Fully Achieved [85%, 100%]:** The course has developed complete knowledge associated with the program objectives.

### E. CLASS RULES

1. Students are expected to have a copy of any of the reference materials. Lectures and exercises are based on these materials.
2. The University rule on class attendance (Article 346 of the University Code) shall be strictly enforced in the class.
3. If a student misses a short quiz, his/her grade on that quiz is zero. If a student misses a long examination for a valid reason (this requires documentation), his/her grade in the final exam will also account for his/her grade for the missed exam. This applies to no more than one long exam missed. A student who fails to take any examination for invalid reasons will get a grade of 0% for that exam.
4. Cheating, in any form, will not be tolerated.

### F. GRADING SCHEME

The work of students shall be graded at the end of each semester/midyear term in accordance with the following system:

Grade	Interval	Classification:
1.00	[96, 100]	Excellent
1.25	[91, 96)	
1.50	[87, 91)	Very Good
1.75	[82, 87)	
2.00	[78, 82)	Good
2.25	[73, 78)	
2.50	[69, 73)	Satisfactory
2.75	[64, 69)	
3.00	[60, 64)	Pass
4.00	[55, 60)	Conditional
5.00	[0, 55)	Fail
INC		Incomplete
DRP		Dropped

Remark: Clearing of Grades of "Incomplete" or "4"

"4" means conditional failure. It may be made up for by successful repetition of the course, or by passing a removal examination. Students are given a grade of "3" if they pass the re-examination, "5" if they fail. Only one re-examination which must be taken within the prescribed time is allowed. If a student does not remove the grade "4" within the prescribed time, he/she may earn credit for the course only by repeating it and passing it.

The grade of "INC" is given if a student whose class-standing throughout the semester is "Passing," fails to take the final examination or fails to complete other requirements for the course due to illness or other valid reasons. In case the class standing is not passing and the student fails to take the final examination for any reason, a grade of "5" is given. Removal of the "INC" must be done within the prescribed time by passing an examination or meeting all the requirements for the course, after which the student shall be given a final grade based on his/her overall performance.

Taken from: [LUPB Academic Catalogue 2019](#)



## G. COURSE OUTLINE

Timeline	CLOs	Topics	Learning Activities	Assessment Tools
<b>PRELIMINARIES (ELEMENTARY PROPERTIES OF INTEGERS)</b>				
Week 1	CLO 1	1. Division Algorithm and Divisibility	Lectures; Group Discussions; Reading Assignments; Individual Inquiry; Consultations; Pause for Reflection;	Quiz Problem Sets; Oral Presentations; Written Examination
Week 2	CLO 2	2. Euclidean Algorithm		
	CLO 3	3. Linear Diophantine Equation		
Week 3	CLO 4	4. Prime Numbers and Their Distribution		
	CLO 5	5. Fermat's Factorization Method		
<b>THEORY OF CONGRUENCES</b>				
Week 4	CLO 2 CLO 3 CLO 4	6. Basic Properties of Congruence	Lectures; Group Discussions; Reading Assignments; Individual Inquiry; Consultations; Pause for Reflection; Collaborative Work; Class Reporting	Problem Sets; Oral Presentations and Reporting; Written Examination
Week 5		7. Fermat's Little Theorem and Pseudoprimes		
		8. Linear Congruences		
Week 6		9. The Chinese Remainder Theorem		
		10. Other Polynomial Congruences		
Week 7	11. Euler Phi Function 12. Multiplicative Functions 13. Tau and Sigma Functions			
<b>PRIMITIVE ROOTS AND INDICES</b>				
Week 8	CLO 1 CLO 4	14. The Order of an Integer Modulo $n$	Lectures; Group Discussions; Reading Assignments; Individual Inquiry; Consultations; Pause for Reflection; Collaborative Work; Class Reporting	Quiz Problem Sets; Oral Presentations and Reporting; Written Examination
Week 9		15. Primitive Roots		
		16. Composite Numbers Having Primitive Roots		
<b>MIDTERM EXAMINATION</b>				
<b>QUADRATIC RECIPROCITY LAW</b>				
Week 10	CLO 4 CLO 5	17. Quadratic Residues and Nonresidues	Lectures; Group Discussions; Reading Assignments; Individual Inquiry; Consultations; Pause for Reflection; Collaborative Work; Class Reporting	Problem Sets; Oral Presentations and Reporting; Written Examination
Week 11		18. The Legendre Symbol and Its Properties		
Week 12		19. Gauss Lemma and the Quadratic Reciprocity Law		
		20. Quadratic Congruences with Composite Moduli		
<b>SPECIAL TOPICS</b>				
Week 13	CLO 1 CLO 4 CLO 5	21. Fermat's Last Theorem	Lectures; Group Discussions; Reading Assignments; Individual Inquiry; Consultations; Pause for Reflection; Collaborative Work; Class Reporting	Problem Sets; Oral Presentations and Reporting; Written Examination
Week 14		22. Continued Fractions		
		23. Infinite Continued Fractions		
Week 15		24. Diophantine Equations		
Week 16		25. Perfect Numbers 26. Applications		
<b>FINAL EXAMINATION</b>				



## H. REFERENCES

1. K. Rosen, *Elementary Number Theory and its Applications, Fifth Edition*, Addison-Wesley, Boston, 2005.
2. D. Burton, *Elementary Number Theory, Sixth Edition*, McGraw-Hill, New York, 2007.
3. R. Carmichael, *The Theory of Numbers*, John Wiley & Sons, New York, 1914.
4. W. Stein, *Elementary Number Theory*, 2004.
5. V. Shoup, *A Computational Introduction to Number Theory and Algebra*, New York University, New York, 2005.
6. R. Guy, *Unsolved Problems in Number Theory, Third Edition*, Springer-Verlag, New York, 2004.
7. N. Robbins, *Beginning Number Theory*, Wm. C. Brown, Iowa, 1993.
8. T. Koshy, *Elementary Number Theory With Applications, 2<sup>nd</sup> ed.*, Netherlands, 2007.
9. G. Everest and T. Ward, *An Introduction to Number Theory (Graduate Texts in Mathematics, Vol. 232)*, Springer, New York, 2005.
10. H. Cohen, *Number Theory Vol II: Analytic and Modern Tools*, Springer, New York, 2010.

## I. RUBRICS FOR ASSESSMENT

### PROBLEM SETS/QUIZZES/ASSIGNMENTS/EXAMINATIONS

CRITERIA	Poor 1	Fair 2	Satisfactory 3	Very Good 4	Excellent 5
<b>Problem Interpretation</b> 30%	Minimal or little indication of ideas relevant to the problem	Correct but insufficient interpretation of the problem	Correct but with significantly inaccurate or unnecessary concepts used in the solution	Correct but with slightly inaccurate or unnecessary concepts used in the solution	Correct and accurate interpretation of the problem
<b>Proof/Solution Correctness</b> 70%	Incorrect or incoherent solution	Logically sound but incomplete solution	Correct solution but with significantly unnecessary steps or insufficient concepts	Correct solution but with slightly unnecessary steps or insufficient concepts	Well-written, logically correct, and clear solution

### ORAL PRESENTATIONS

CRITERIA	Poor 1	Fair 2	Satisfactory 3	Very Good 4	Excellent 5
<b>Content Knowledge</b> 50%	Little understanding of the topic	Understands the topic but unable to answer the audience's questions	Familiarity of the topic, answers few or some of the audience's questions	Familiarity of the topic, answers the audience's questions elaborately	Mastery of the topic, discusses minimum key points with the most impact, answers the audience's questions elaborately
<b>Delivery</b> 20%	No script, incomprehensible and inaudible voice	Unfamiliarity of script, clear but monotone voice with several mispronunciations of terms	Familiarity of script, clear voice with few mispronunciations of terms	Familiarity of script, clear voice with correct pronunciation of terms	Mastery of script, clear voice with correct pronunciation of terms
<b>Visuals</b> 15%	Too much text with no visual aids, unreadable presentation with irrelevant information, several typographical errors	Readable presentation but with little visual aids, several typographical errors	Readable presentation, and uses some visual aids vital to the presentation, few typographical errors	Comprehensive presentation, makes use of appealing visual aids vital to the presentation, no typographical error	Comprehensive presentation, makes use of appealing, effective and varying visual aids vital to the presentation, no typographical error



<b>Organization</b> 15%	Untimely and unstructured presentation delivery with no logical flow of information	Structured but with confusing flow of information, or untimely presentation delivery	Structured with logical flow of information, or untimely presentation delivery	Well-structured, timely presentation delivery with logical flow of information	Well-structured, timely presentation delivery with logical and interesting flow of information
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## THE UNIVERSITY OF THE PHILIPPINES

UP was founded in 1908 with its first campus in Manila. It was followed soon after by the establishment of constituent universities and campuses all over the country. Over the course of a century, UP has established eight constituent universities distributed across 17 campuses.

### Vision

The University of the Philippines (UP) envisions itself to be a leading regional and global university in an environment that sustains 21st-century learning, knowledge, creation, and public service for society and humanity.

### Mandates

As the national university, UP is mandated to perform its unique and distinctive leadership in higher education and development, in terms of:

- Setting academic standards and initiating innovation in teaching, research, and faculty development in an environment of academic freedom;
- Serving as a graduate university providing advanced and specialized studies, especially to the faculty members of state and private colleges and universities;
- Serving as a research university in various fields of expertise and contributing to the dissemination and application of new knowledge;
- Leading as a public service university by providing different forms of community, public, and volunteer service to the government, the private sector, and civil society;
- Protecting and promoting the professional and economic right and welfare of its academic and non-academic personnel;
- Providing learning opportunities in various forms to promote such special concerns as responsible citizenship, sustainable development, sports and health development, and cultural development;
- Serving as a hub for regional and global academic networks; and
- Applying the highest standards of academic and institutional governance within a meritocracy based on collegiality, representation, accountability, transparency, and active participation of all constituents.

For more information on the University's Vision and Mission, refer to the [UP Strategic Plan 2017-2023](#).

### University of the Philippines' Philosophy of Education and Graduate Attributes

A UP education seeks to produce graduates imbued with an abiding sense of responsibility to their people and nation, the skills and mindsets to improve human life, and a commitment to the freedom and welfare of all.

Aside from mastery of knowledge in their specific disciplines, UP graduates must possess breadth of mind, strength of character, and generosity of spirit, fostered by a firm grounding in both the arts and sciences, and such specialist courses as their programs may require.

They must be prepared to inclusively engage with society and the world at large, mindful of their people's needs and capabilities, and keen to the challenges and opportunities of national development in this century of rapid global change.

UP aims to achieve this through its General Education program, one that develops mind, body and spirit, which familiarize all its students with their culture and history and fosters a sense of shared citizenship, while equipping them with critical thinking, discernment and technical skills they will need to excel in their chosen professions.



## THE UNIVERSITY OF THE PHILIPPINES BAGUIO

Established through the initiative of UP alumni in Baguio and Benguet, the University of the Philippines Baguio was inaugurated as a degree-granting unit of the University on 22 April 1961. A land grant worked out by alumni, the City Council, and by then UP President Vicente Cinco situated the College on its present location, a pine clad-hill offering a scenic view of Baguio. The College went on to make its presence felt as it served as the site of the National Arts Festivals in the coming years. Moves were made to strengthen its research capabilities, culminating in the institution of the Cordillera Studies Center in 1983. Directions towards autonomy began with strategic planning in 1996. The following years saw the College working assiduously in the reformulation and strengthening of its academic programs, primarily. Administration of the College likewise oversaw the development in infrastructure and improvement of services and facilities. Such growth led to the elevation of UP College Baguio to full autonomous status, granted by the Board of Regents in December 2002. UP Baguio is now the seventh constituent university of the UP System.

### Vision

As a constituent university of the University of the Philippines System, UP Baguio will sustain its lead position in the delivery of tertiary education in the north. It will continue to nurture and develop innovative programs in the arts and sciences. It will also continue to develop the niche it has created over the past decades in Cordillera Studies.

### Mission

Our mission, therefore, as a unit of the U.P. System and as the leading institution of higher learning in Northern Luzon, is to spearhead the offering of the highest standard of education and to contribute to the overall upgrading of the quality of instruction in the region. We seek to create an impact by informing our programs with a regional perspective, at the same time that these are informed by a national and global outlook.

For more information on UP Baguio's Vision and Mission, refer to the [official UP Baguio webpage](#).

## THE COLLEGE OF SCIENCE

After the reorganization of UP Baguio during its institution as the seventh constituent university of the UP system in 2002, the College of Science (CS), being one of the three colleges emerging from the reorganization, evolved from the merger of the Division of Natural Sciences and Mathematics and the Sports, Physical Education and Recreation Division. The College offers four undergraduate degree programs: BS Biology, BS Computer Science, BS Mathematics, and BS Physics program. All these programs are regularly reviewed and upgraded to prepare students for careers in education, research, or postgraduate studies.

The CS Dean, together with the Faculty Assembly and in cooperation with the College Executive Board (CEB), leads the Department of Biology, the Department of Physical Sciences, the Department of Mathematics and Computer Science, and the Human Kinetics Program towards academic excellence and public service.

### Vision

The College of Science aims to continue offering high standard and relevant quality education through good practices in program implementation that follow innovative pedagogical strategies that utilize appropriate technology in supporting this endeavor. It will further its objectives by initiating interdisciplinary programs anchored on disciplinary specializations in its efforts to enhance the efficiency of research conduct and management. It will continue to encourage and reward scientific productivity by conducting research responsive to the needs of the region, nation, and the global community.

The College envisions itself moving towards a more inclusive and equitable environment that enables faculty members to lead on with exemplary qualifications – mindful of scholarly research and dedicated to public service.





Furthermore, it will support UP Baguio's wellness program for both academic and support staff to guarantee efficiency in service to the university and the society.

Lastly, the College, together with the University, will take initiative to continue, strengthen and widen the reach of its involvement in public service by sharing individual and collective expertise with other academic institutions, local government units, NGOs, peoples' organizations, and indigenous communities in the region and other areas.

### **Mission**

In line with the college's vision, it is our mission, therefore, to produce scientific leaders and civic-minded citizens with high regard for integrity, compassion, and genuine service who lead in a research study that follows ethical standards and excellence in instruction, research, and public service.

It is our mission to improve on basic facilities and design where researchers can work more collaboratively and efficiently. We pursue to guarantee the safety of researchers, to minimize adverse impact to the environment, to respect research protocols involving indigenous communities, and to ensure professional conduct as we encourage good instruction, research, and public service in upholding the University's banner of *Honor and Excellence*.

### **Goals**

In accordance with the mission and vision of the University, the college aims to accomplish the following goals:

- To continue formulating new degree programs while regularly upgrading existing ones;
- To encourage interdisciplinary research across programs;
- To institutionalize the Science Research Center in continuing research responsive to the need of the region, and in the enhancement of interdisciplinary collaboration within the departments of the College and even with other faculty members in other colleges of the University of the Philippines Baguio;
- To have a closer linkage with the Cordillera Studies Center as the university's research center and as an aid in putting up the biodiversity and innovation research center;
- To foster an environment suitable for the growth of the academic and support staff; and,
- To provide public service based on each academic and support staff's specialization.

For more information on CS' Vision, Mission, and Goals, refer to the [official CS website](#).

## **THE DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE**

The Department of Mathematics and Computer Science (DMCS) grew from a discipline to a department in 2002 when UP Baguio became the seventh constituent university of the UP System. The Department offers two undergraduate programs (BS Mathematics and BS Computer Science) and two graduate programs (MS Mathematics and PhD Mathematics). The Department pioneered the PhD Mathematics Program in Northern Luzon.

### **Vision**

The DMCS adheres to the highest standards of excellence in all aspects of teaching, research, and extension service. It will build and maintain nationally and internationally recognized experts in the core and emerging areas of study in mathematics, statistics, and computer science. It will set the standards for promoting quality instruction, interdisciplinary research, teacher training, and other extension programs within the University, the Northern Luzon region, and the country.

Further, it aspires to become a Center of Excellence in mathematics both in the country and in the ASEAN region.



## Mission and Goals

The DMCS is committed to pursuing excellence in teaching, research, and extension service within the University, the Northern Luzon region, and the country.

The Department identified these five major goals to help realize its mission:

1. Strengthen its graduate and undergraduate programs;
2. Aggressively promote and maintain high standards of quality education;
3. Lead in research capability building and research-generating activities in the mathematical and computing sciences and in mathematics education in the region;
4. Upgrade the quality of mathematics and computing education in the primary, secondary, and tertiary levels in Northern Luzon; and
5. Make quality mathematics and computer science education accessible to the people in the region.

## The MS Mathematics Program

The Master of Science in Mathematics (MS Math) Program of UP Baguio, instituted in 2001, provides students with a firm grounding in theoretical Mathematics to prepare them for doctoral studies, research, careers in industry and government, and for teaching junior and senior level undergraduate Mathematics courses.

The MS Math curriculum is designed to allow the student an in-depth study of standard graduate courses in Analysis and Algebra, and electives that would lead the student to a specialization area of Mathematics in preparation for his/her research work. The curriculum also helps the student in applying mathematical tools to problems in other disciplines, such as Engineering, Physics, Life Sciences, Computing Sciences, Statistics, Finance and even the Social Sciences.

*For more information on DMCS' Vision, Mission and Goals, and the MS Mathematics Program, refer to the [official DMCS website](#).*

Updated as of April 2023